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To cite this article before publication: David Bolst *et al* 2019 *Phys. Med. Biol.* in press <https://doi.org/10.1088/1361-6560/ab586a>

Manuscript version: Accepted Manuscript

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Validation of Geant4 for silicon microdosimetry in heavy ion therapy

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Abstract. Microdosimetry is a particularly powerful method to estimate the relative biological effectiveness (RBE) of any mixed radiation field. This is particularly convenient for therapeutic heavy ion therapy (HIT) beams, referring to ions larger than protons, where the RBE of the beam can vary significantly along the Bragg curve. Additionally, due to the sharp dose gradients at the end of the Bragg peak (BP), or spread out BP, to make accurate measurements and estimations of the biological properties of a beam a high spatial resolution is required, less than a millimetre. This requirement makes silicon microdosimetry particularly attractive due to the thicknesses of the sensitive volumes commonly being $\sim 10 \mu\text{m}$ or less. Monte Carlo (MC) codes are widely used to study the complex mixed HIT radiation field as well as to model the response of novel microdosimeter detectors when irradiated with HIT beams. Therefore it is essential to validate MC codes against experimental measurements.

This work compares measurements performed with a silicon microdosimeter in mono-energetic ^{12}C , ^{14}N and ^{16}O ion beams of therapeutic energies, against simulation results calculated with the Geant4 toolkit. Experimental and simulation results were compared in terms of microdosimetric spectra (dose lineal energy, $d(y)$), the dose mean lineal energy, y_D and the RBE_{10} , as estimated by the microdosimetric kinetic model (MKM). Overall Geant4 showed reasonable agreement with experimental measurements. Before the distal edge of the BP, simulation and experiment agreed within $\sim 10\%$ for y_D and $\sim 2\%$ for RBE_{10} . Downstream of the BP less agreement was observed between simulation and experiment, particularly for the ^{12}C and ^{16}O beams. Simulation results downstream of the BP had lower values of y_D and RBE_{10} compared to the experiment due to a higher contribution from lighter fragments compared to heavier fragments.

Keywords: Microdosimetry, Heavy ion therapy (HIT), Silicon-on-insulator (SOI), Geant4, Validation

1. Introduction

Heavy ion therapy (HIT), referring to ions heavier than protons for cancer treatment, has had growing interest in recent years due to its potential for greater dose conformity over both conventional photon X-ray and proton therapy [1]. HIT is also attractive for radioresistant tumours, such as osteosarcomas [2], since HIT does not rely on the production of free radicals nearly as much as conventional radiotherapy. With conventional X-ray radiotherapy having an oxygen enhancement ratio (OER) of ~ 3 and ions larger than ^{12}C having an OER of ~ 1 [3]. A lower OER has the potential to make tumours with hypoxic regions simpler to treat by not having to know the concentration of oxygen/blood as accurately or account for changes over time. The advantages of a higher LET also brings with it some complications, for therapeutic heavy ions, such as ^{12}C , where the LET varies from ~ 10 - $1000\text{ keV}\mu\text{m}$ [4], resulting in a relative biological effectiveness (RBE) which varies significantly along the Bragg curve. For successful treatment with HIT it is essential to account for the varying RBE in order to produce a uniform biological dose treatment to the target volume [5].

There are several theoretical methods capable of predicting the changing biological effectiveness in HIT, such as the Local Effect Model (LEM) [6] which uses cell survival data of photons with the track structure of ions. Models such as these calculate the biological effect of the beam theoretically and are not based on making experimental measurements of the ion beam directly. For quality assurance, it is important to be able to directly measure the properties of a delivered beam experimentally and ensure that the properties of the delivered beam match those of the planned beam. One such method to estimate the RBE of an ion beam experimentally, is with microdosimetry and the microdosimetric kinetic model (MKM) [7]. Microdosimetry is the study of energy deposition in micron sized sensitive volumes (SVs) [8], representing the size of cell structures. Microdosimetry measurements are conventionally performed using tissue equivalent proportional counters (TEPCs), with commercial solutions often having a physical SV (not simulated) of the order of $\sim 10\text{ mm}$ in diameter [9]. These relatively large volume sizes are not ideal for making measurements of the distal edge of a Bragg peak/spread out Bragg peak (BP/SOBP). Silicon microdosimeters provide a much higher spatial resolution, with SV thicknesses of $\sim 10\ \mu\text{m}$ and less commonly being used in hadron therapy beams [10] [11].

Due to the complexity of the radiation field in HIT, with $\sim 70\%$ of a $400\text{ MeV/u }^{12}\text{C}$ ion beam undergoing a nuclear reaction before the BP [12], Monte Carlo simulations are often performed to study the radiation field and for comparison against experiment [13]. As such, it is important to know the performance of the physics models used in the Monte Carlo simulation compared to dedicated experimental measurements. This work evaluates the performance of the Monte Carlo toolkit Geant4 [14] [15] [16], for modelling silicon microdosimetry in HIT radiation fields against experimental measurements performed at the Heavy Ion Medical Accelerator in Chiba, (HIMAC), Japan. The studied beams include mono-energetic ^{12}C , ^{14}N and ^{16}O ions. Comparisons between the experiment and simulation are performed in terms of the: microdosimetric spectra, dose mean lineal energy (y_D) and the RBE_{10} , as estimated by the modified microdosimetric kinetic model (MKM) [7].

2. Materials and Methods

This work compares experimental measurements obtained using a silicon microdosimeter against simulation results using the Monte Carlo toolkit Geant4, version 10.2p3. The experimental measurements were obtained at the Biological beamline in HIMAC, Japan, which is briefly described in section 2.1. The silicon microdosimeter used was the first generation Mushroom air-trenched microdosimeter, designed by the Centre for Medical Radiation Physics (CMRP) and fabricated by SINTEF [17], and is described in section 2.3. The Mushroom microdosimeter was irradiated with mono-energetic ^{12}C , ^{14}N and ^{16}O ion beams separately, with energies of 290 MeV/u , 180 MeV/u and 400 MeV/u , respectively. The experimental ^{12}C ion measurements

were originally presented in [10] by Tran et al. and the ^{14}N and ^{16}O ion results by Tran et al. in [11].

The setup of the experiment and the simulation is shown in figure 1, which shows the Mushroom microdosimeter placed in a water proof sheath (described in section 2.2), in a water phantom with 6 mm thick PMMA walls, placed at the iso-centre of the Biological beamline. The water phantom has an area of $220 \times 220 \text{ mm}^2$ perpendicular to the beam and a thickness of 260 mm. The microdosimeter was positioned in the centre of the beam (X-Z plane) and was moved through the radiation field in the Y-direction by a motion stage, which allows the position to be placed within an accuracy of a mm.

The electromagnetic interactions were modelled using the *G4 Standard EM option 3* physics constructor. The High Precision (HP) Data library was used to model neutron physics processes below 20 MeV. The simulations were run two separate times with alternative inelastic hadronic models used to compare to one another. The hadronic interactions of ions were modelled by the *G4IonBinaryCascadePhysics* (BIC) model and the *G4IonQMDPhysics* (Quantum Molecular Dynamics-QMD) model. These models were recently validated against experimental measurements of the fragmentation of a ^{12}C ion beam [18].

2.1. The Biological beamline

The Biological beamline at HIMAC, shown in figure 1, has been previously modelled in Geant4 and validated for mono-energetic and spread out Bragg peak ^{12}C ion beams by Bolst et al. [19]. It consists of a mono-energetic pencil beam which is shaped by a pair of two wobbling magnets into a circular shape. The lateral dose uniformity of the beam is then improved by passing through scatterers (tantalum in this study) and the neutron contribution in the beam is reduced by a neutron shutter. The beam is shaped by various collimators after the neutron shutter, with the final collimation being performed by a pair of 5 cm thick brass X-Y collimators. For this study of mono-energetic beams, the ridge filter shown in figure 1 is not used.

The beamline parameters simulated for the three different ion beams considered (^{12}C , ^{14}N , ^{16}O) and their BP position in the water phantom are summarised in table 1. All beams were collimated to $100 \times 100 \text{ mm}^2$ by the X-Y brass collimators just before the phantom. For the ^{12}C ion beam, the magnetic amplitude of the wobbler magnets (B_0) was set to 0.045 T. The ^{14}N and ^{16}O ion beams, instead of simulating the complete wobbler configuration, used a diverging source, or a “cone” beam, with a divergence of 0.5° . The use of a diverging beam was previously found in [19] to not significantly affect the energy deposition along the centre of the beam, with a difference within $\sim 0.2\%$ along the entire water phantom. In addition to the increased simplicity of the cone beam, this approach was used due to the lack of lateral dose measurements which are required to finely tune the wobbler strength. The ^{16}O ion beam is the only beam to use PMMA range shifters, with a total thickness of 86 mm or a water equivalent thickness (WET) of ~ 100 mm and are positioned approximately 300 mm upstream from the water phantom. The range shifter was used because the beam’s range was too large (~ 190 mm) to study the BP region in the water phantom. Despite the use of the range shifter, the range of the ^{16}O ion beam are quoted with reference to the depth in the water phantom itself and does not add the additional 100 mm WET of the range shifter.

2.2. Water proof sheath and probe

The water proof PMMA sheath, placed in the water phantom, houses the micro-plus (μ^+) probe, which is an in-house CMRP designed and built probe which provides a compact and low noise readout system. A screenshot of the PMMA probe, modelled in Geant4, is shown in the bottom left diagram of figure 1. The PMMA sheath is modelled as a $30 \times 30 \times 30 \text{ mm}^3$ block covered with a $75 \mu\text{m}$ thick aluminium layer except above the window (see diagram). At the far left of the PMMA sheath, where the beam is incident, there is a $16 \times 16 \text{ mm}^2$ cutout which is 4.7 mm

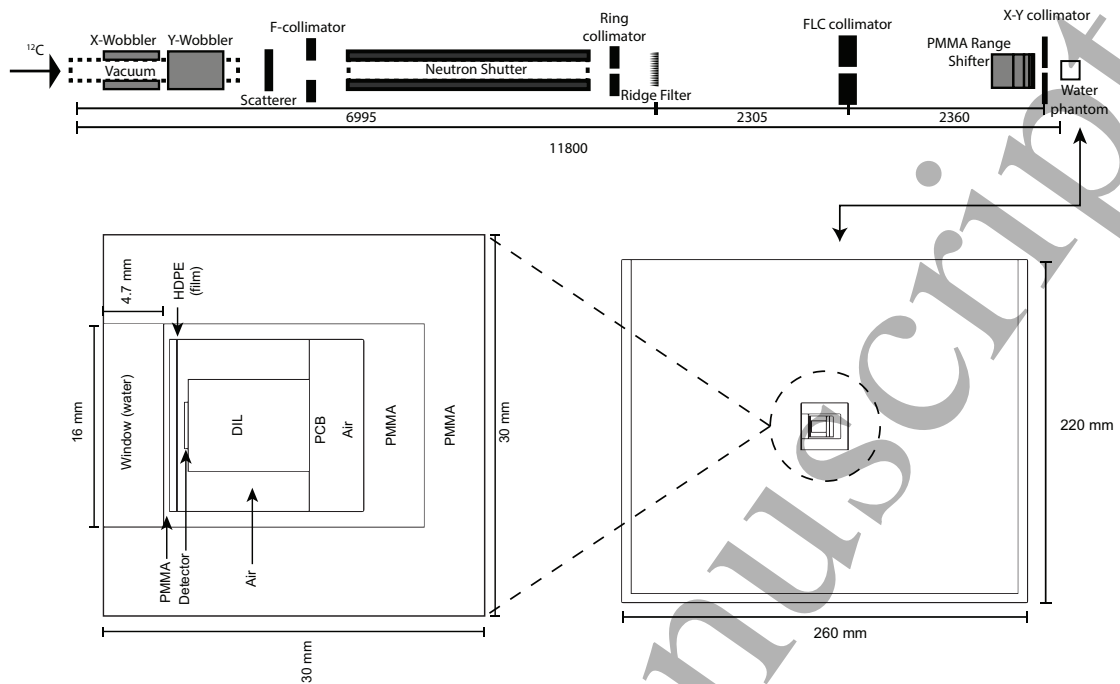


Figure 1: Top: Layout of the Biological beamline modelled in Geant4, not to scale, figure reproduced from [19]. Bottom right: Enlarged view of the water phantom containing the detector probe. Bottom Left: Enlarged view of the water proof probe encasing the detector.

Ion	Primary Energy (MeV/u)	Energy Sigma (%)	Ta Thickness (mm)	Range shifter (mm)	BP in phantom (mm)
^{12}C	288.6	0.2	0.434	0	149
^{14}N	180	0.36	0.434	0	49
^{16}O	400	0.15	0.649	86	91.5 (191.5)

Table 1: Summary of the configurations of the ion beams and their Bragg Peak (BP) positions considered in this work. The second value of 191.5 mm for the BP position in ^{16}O adds the 100 mm of WET provided by the PMMA range shifter.

deep. This cutout is done to minimise non-water material inline of the beam, with the water proof sheath only adding a 0.5 mm thickness of PMMA to the beam before the detector. Right of the 0.5 mm thick PMMA window there is 0.5 mm of air before a 0.1 mm thick high density polyethylene (HDPE) film which shields the detector from visible light. Beyond the HDPE film there is another 0.53 mm of air just before the surface of the Mushroom microdosimeter. The detector is mounted onto an aluminium oxide dual in-line (DIL) package which is on a PCB modelled as pyrex glass.

When measurements are made using the water proof sheath, the reported “depth” is given in terms of the water equivalent thickness (WET) from the face of the water phantom (6 mm of PMMA) to the surface of the detector. This involves using conversion factors, calculated using Geant4 by simulating the BP positions for different beam energies and materials. The conversion factor is calculated by taking the ratio of the BP position in water to the other material, which is similar to taking the average ratio of the stopping powers of the two materials. The materials before the detector and their thicknesses, as well as their converted WETs are shown in table 2.

Item	Material	Thickness (mm)	Conversion factor	WET (mm)
Water phantom wall	PMMA	6	1.16	6.96
Probe window	PMMA	0.5	1.16	0.58
Top air gap	Air	0.53	0.001	0.00053
Film	HDPE	0.1	1	0.1
Bottom air gap	Air	0.53	0.001	0.00053

Table 2: Summary of the different materials, their thicknesses and WETs from the start of the water phantom case to the face of the detector.

2.3. Air trenched Mushroom microdosimeter

The Mushroom microdosimeter was modelled in Geant4 based on the images obtained with a scanning electron microscope (SEM) [20]. Diagrams and images of the Mushroom are shown in figure 2, with the top right being an SEM image and the remaining diagrams being screenshots from the Geant4 simulation. This device is the first generation of its design used by CMRP and exploits 3D technology [21], which has the advantages of: radiation hardness, fast collection times, well defined SVs and low depletion voltages [22].

The Mushroom is fabricated from a high-resistivity p-type silicon of 10 k Ω cm and the structural design is referred to as a trenched 3D. The SV has a trenched hollow core and hollowed semi-circles which extend $\sim 2.7 \mu\text{m}$ from the SV to reduce charge generated outside of the SV from being collected. The SVs cover an area of $\sim 2.5 \times 2.5 \text{ mm}^2$ and are connected into arrays of 50 \times 50 rows and columns by aluminium contacts. The SVs have a thickness of 9.1 μm and a diameter of 28.5 μm . On the top surface of the SV there is a 0.85 μm thick overlayer of SiO₂ directly on top of the silicon. On the bottom of the silicon SV there is also a 0.85 μm thick SiO₂ insulator layer which is above a 300 μm thick silicon substrate. The aluminium contacts which connect the SVs together into arrays were modelled as having a width of 3.75 μm and thickness of 1 μm . More extensive details of the Mushroom microdosimeter as well as experimental and theoretical characterisation of the device can be found in [20].

Every ion beam was measured with a slightly different energy channel calibration. For both the ¹²C and ¹⁶O ion beams, 4096 energy bins were used with a minimum energy deposition of 32.8 and 25.5 keV, respectively; while their maximum energy deposition was 22371.6 and 22322.2 keV, respectively. For the ¹⁴N ion beam 8192 energy bins were used instead, with a minimum and maximum energy deposition of 15.8319 and 22314.5 keV, respectively. For visual purposes the original linear bins were re-binned into 110 logarithmically spaced bins with a lineal energy range from 0.1-10000 keV/ μm .

2.4. Microdosimetric quantities compared between experiment and simulation

The quantities used to compare simulation and experiment in this work are the dose mean lineal energy, y_D , and the relative biological effectiveness at 10% survival, RBE₁₀. The quantities are compared between simulation (Sim) and experiment (Exp) by using the percentage difference, PD , as defined in equation 1. In addition to comparing these two quantities, the microdosimetric spectra are also compared qualitatively in terms of their shape and peak positions.

$$PD = \left(\frac{Exp - Sim}{Exp} \right) \times 100\% \quad (1)$$

Equation 2 is used to calculate the lineal energy, y , from the energy deposition, E , in the the Mushroom microdosimeter. The κ coefficient converts the energy deposited in the silicon SV to a material representing a tissue equivalent medium (striated muscle in this work). In this work κ is fixed to 0.57 based on the work by [23]. The lineal energy is calculated by using the mean

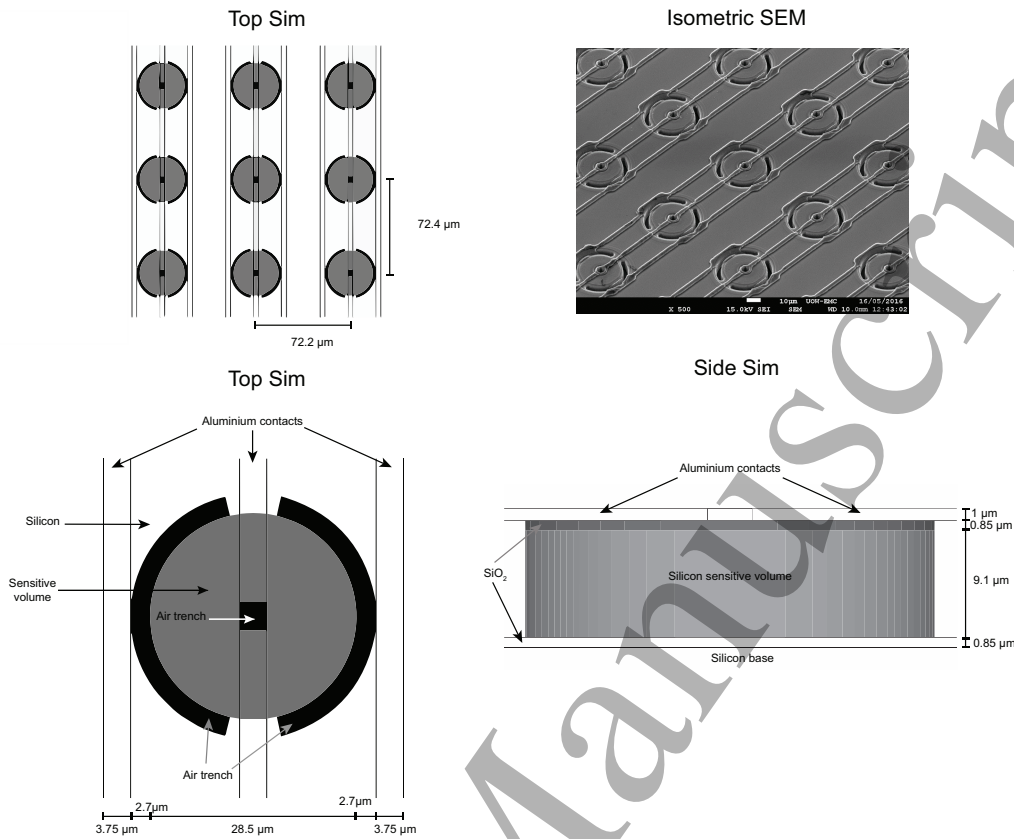


Figure 2: The Mushroom microdosimeter modelled in Geant4 and an SEM image (top right) of the real world device.

path length of the silicon SV ($\langle l_{Path,Si} \rangle$) instead of the traditional mean chord length calculated using Cauchy's equation, which is valid only for isotropic fields. The mean path length was demonstrated to be more appropriate in [23] to calculate the lineal energy in HIT beams due to their high directionality of HIT beams. Additionally, for simplicity the mean path length is fixed in this study, equal to the thickness of the SV, $9.1 \mu\text{m}$, based on [23].

The probability distribution of the lineal energy (equation 2) is denoted as $f(y)$. The dose mean lineal energy, y_D , is the ratio of the second and first moments of $f(y)$ and is shown in equation 3.

$$y = \frac{\kappa E}{\langle l_{Path,Si} \rangle} \quad (2)$$

$$y_D = \frac{\int y^2 f(y) dy}{\int y f(y) dy} \quad (3)$$

The RBE_{10} at different positions in the beam was estimated using the modified MKM, which uses the measured microdosimetric spectrum ($f(y)$) as input to the model. The MKM was originally formulated by Hawkins in 1994 [24] and is based on dividing the cell nucleus into sub-nuclear sites called "domains" and assumes that the response of these domains from radiation follows a linear quadratic curve. The MKM was later modified by Kase et al. [7] to account for

over-killing effects, which is important for HIT. The output from the MKM is an estimated cell survival response from radiation (RBE_{10}) for a particular cell. In order to make this prediction, certain cell specific parameters must be measured such as the parameters of the linear-quadratic model of cell survival, α_0 and β for photon irradiation. The α_0 and β parameters describe the response of cells when irradiated with different amounts of dose, with α_0 describing the initial response of cells at lower doses and β describing the response at higher doses [25]. In addition to α_0 and β , the domain “size” (r_d) and the LET where over-killing begins for the cell type are also required in order to predict the cells’ response. In this work, the estimated RBE_{10} is calculated for human salivary glands (HSG) cells, using cell parameters measured by Kase et al. [7]. The α_0 and β values measured for HSG cells were 0.13 Gy^{-1} , 0.05 Gy^{-2} , respectively, while the domain radius had a value of $0.42 \text{ }\mu\text{m}$ with an assumed density of tissue of 1 g/cm^3 (ρ in the equation below). Finally, the LET of radiation where over-killing effects begins was determined to be $150 \text{ keV}/\mu\text{m}$ and is called the saturation parameter and labelled as y_0 in the modified MKM. Once y_0 is determined for a particular cell the saturation-corrected dose mean lineal energy, y^* , can be calculated using the measured microdosimetric spectrum and equation 4. From y^* the α value can be calculated from equation 5 and then the estimated RBE_{10} can be calculated using equation 6, where $D_{10,x-ray}$ is the dose needed to obtain a 10% cell survival of HSG cells for a 200 kVp x-ray source and was measured by Kase et al. to be 10 Gy.

$$y^* = y_0^2 \frac{\int (1 - \exp(-y^2/y_0^2)) f(y) dy}{\int y f(y) dy} \quad (4)$$

$$\alpha = \alpha_0 + y^* \frac{\beta}{\rho \pi r_d^2} \quad (5)$$

$$RBE_{10} = \frac{2\beta D_{10,x-ray}}{\sqrt{\alpha^2 - 4\beta \ln(0.1)} - \alpha} \quad (6)$$

In order to obtain sufficient statistics, in the form of “hits” or counts in the microdosimeter, the number of primary ion particles generated in the simulation was varied depending on where along the beam the microdosimeter was positioned. For positions upstream of the BP the number of primary ions generated varied between ~ 1 and 2×10^7 , while for positions at the pinnacle and distal edge of the BP 2×10^7 primary ions were generated. Due to the loss of the primary beam, positions downstream of the BP had $\sim 10^8$ primary ions generated. The error bars plotted in this work only reflect the statistical error in the number of counts in the channels of the detector and do not consider any other uncertainties, such as cell specific parameters for the estimated RBE_{10} . The uncertainty of the simulation is calculated by splitting the total number of counts recorded in the detector into ten groups and taking the standard deviation of the quantity of interest (y_D or RBE_{10}) and is plotted with a 68% confidence limit. The error bars associated with the experiments are based on error propagation, with the starting error being the square root of the counts in each bin. The error bars displayed on the microdosimetric plots are calculated the same way for both the experiment and the simulation and are based on the number of counts in each logarithmically spaced bin.

3. Results

For the results presented below the comparisons between simulation and experiment are primarily with respect to the BIC model, with discussion of QMD results left for the Discussion section (section 4). The microdosimetric spectra (figures 3, 5 and 8) shown below are all generated with the BIC model, where “Total” and each particle’s contribution to the spectrum refers to the BIC model’s response. However, for these three figures there is one plot corresponding to 5 mm downstream of each beam’s BP, where “Total” and each particle’s

spectra for each particle refers to the QMD model, with the total BIC response also plotted for reference.

3.1. Mono-energetic 290 MeV/u ^{12}C ion beam

The dose weighted microdosimetric spectra, displayed on the traditional semi-log scale, $y_D(y)$, at various depths in the water phantom along the mono-energetic ^{12}C ion beam and downstream of the BP, are shown figure 3. The top left plot shows the microdosimetric spectra at the entrance of the phantom (18.91 mm) while 149 mm corresponds to the pinnacle of the BP. The contribution to the total dose deposited in the detector by different particle types in the simulation is also plotted. The ^{12}C ion peak (dashed green line) on the right of the spectra is observed to dominate the spectra, with secondary fragments only making noticeable contributions at the distal part of the BP and beyond, as expected.

From the entrance of the phantom to the pinnacle of the BP, the lineal energy of the ^{12}C peak increases from ~ 10 to ~ 100 keV/ μm , with a stopper peak at the far right of the spectrum with a lineal energy of ~ 700 keV/ μm . At the end of an ion's range, its LET increases rapidly, meaning that a small change in depth of a few 100 microns can drastically change the value of y_D . This rapid change in LET, together with the sharp dose gradients at the end of an ion's range, means that with the current positional uncertainty in the water phantom of ~ 1 mm, at the distal edge of the BP the agreement between experiment and simulation is harder to achieve.

After the incident beam has stopped, the microdosimetric spectrum is significantly different as it is produced by the secondary mixed radiation field only. The lineal energy peaks of the microdosimetric spectrum at 155 mm (6 mm distal from the BP pinnacle) can be seen to align reasonably well when comparing simulation results and experimental measurements, with the most prominent peak being mostly from boron fragments. However, at the lower lineal energies the simulation is seen to have an excessive proportion of lighter fragments compared to larger fragments, with ^4He being very dominant in the simulation.

The calculated values of y_D and RBE_{10} , using the MKM, are shown in figure 4. The right plots show an enlarged view of the BP region of the left plots. For reference, the energy deposition scored in 0.1 mm thick water slabs along the phantom by the simulation (without the detector/probe present) is plotted in red.

Comparing the y_D values of experiment and simulation, excellent agreement is observed for both the values and the shape, particularly at the BP. Upstream of the BP region, the y_D is seen to be fairly constant with a value of ~ 20 keV/ μm reaching a maximum of 250 keV/ μm (simulation) to 300 keV/ μm (experiment). It can be seen that for a few depths upstream of the BP, particularly at 18.91 mm, that the error bars of the simulation are quite large compared to other depths. This large error bar occurs due to a few high LET particles depositing energy in the SV. Downstream of the BP the simulation is consistently lower than the experiment. Which as discussed with the microdosimetric spectra in figure 3, the simulation is characterised by an overproduction of lighter fragments (mostly likely He fragments) with respect to heavier fragments.

For RBE_{10} values the agreement is slightly better than the y_D results, with the difference being $\sim 2\%$ before the distal part of the BP. The RBE_{10} has noticeably less fluctuations than y_D , this can be attributed to y_D being proportional to y^2 while RBE_{10} is proportional to $(1 - \exp(-y^2/y_0^2))$. This causes infrequent, high y events, to have a much greater influence on y_D compared to RBE_{10} , particularly when y is over 150 keV/ μm (the saturation parameter value used by the modified MKM). At the entrance of the phantom the RBE_{10} is ~ 1.17 and reaches a maximum at the pinnacle of the BP with a value of ~ 2.9 .

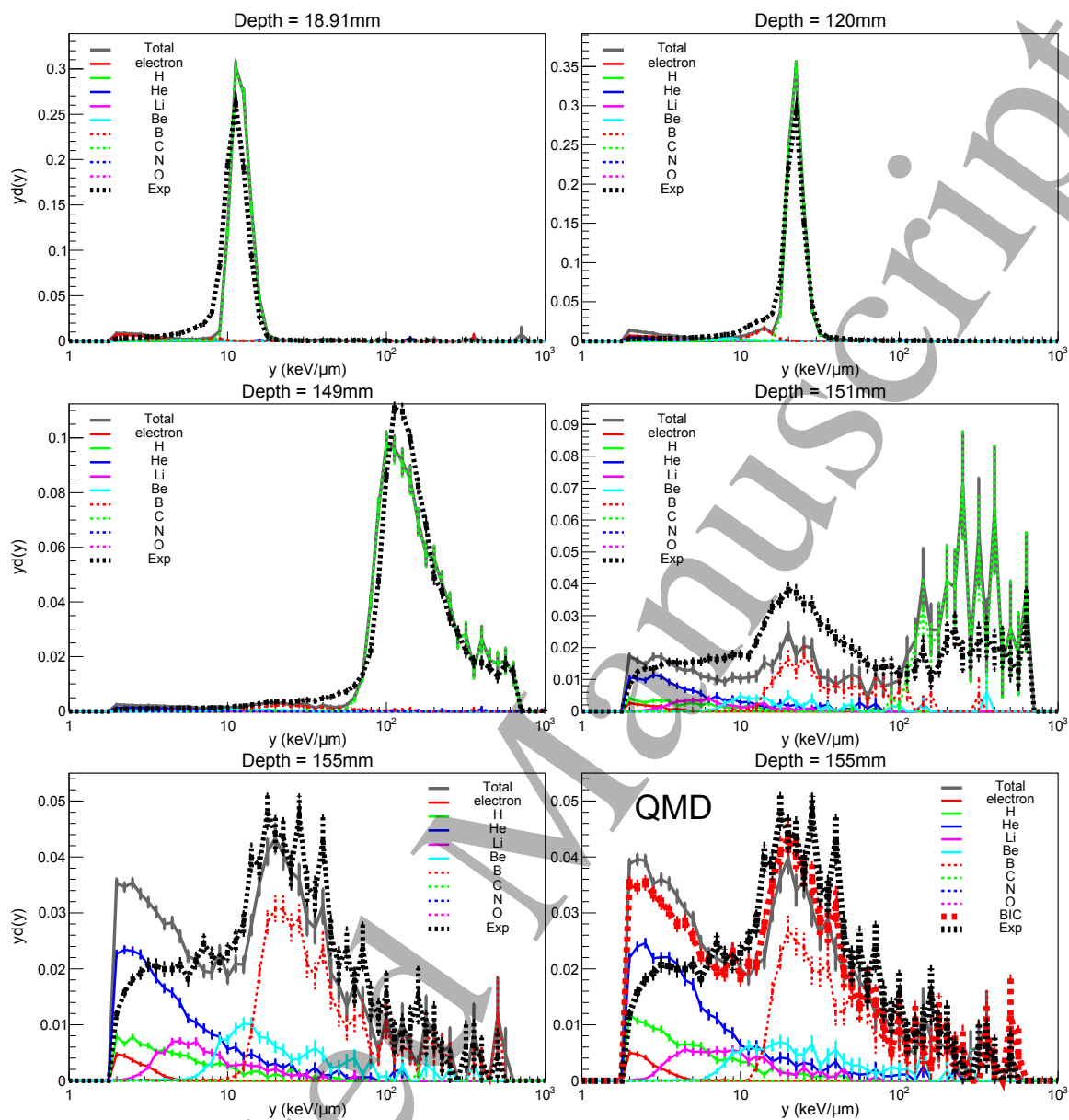


Figure 3: Comparison between the microdosimetric spectra calculated with Geant4 (continuous line) and the experimental measurements (dashed line) at different depths along a 290 MeV/u ^{12}C ion beam in a water phantom. All simulation spectra shown are obtained with the BIC model except for the 155 mm depth labelled with “QMD”, which was calculated with the QMD model.

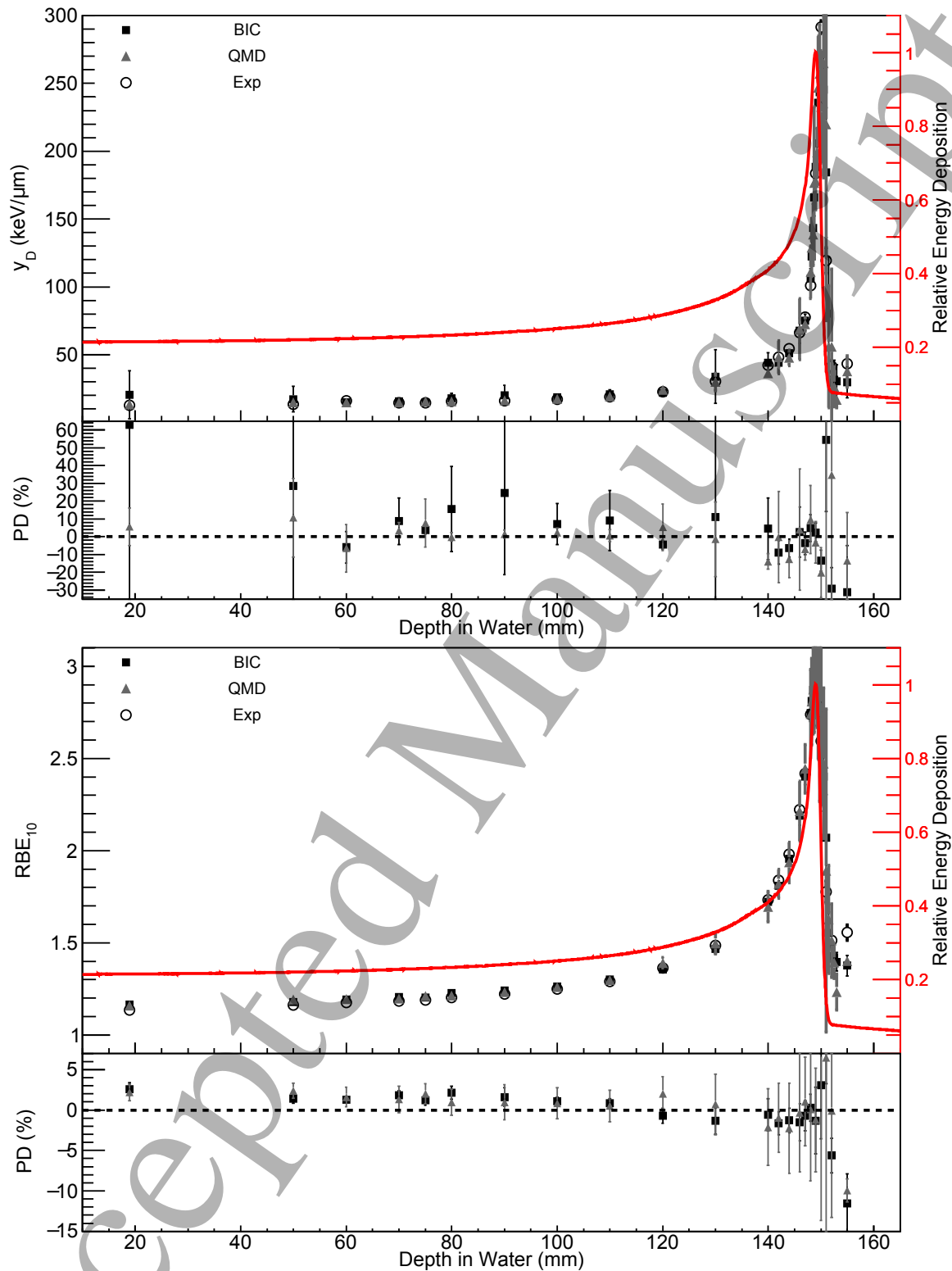


Figure 4: Calculated y_D (top) and RBE_{10} (bottom) values in the 290 MeV/u ^{12}C ion beam using both the measured and simulated spectra from the Mushroom microdosimeter. The lower panels in both graphs show the percentage deviation (PD) between both data sets.

3.2. Mono-energetic 180 MeV/u ^{14}N ion beam

A selection of microdosimetric spectra at different depths in the water phantom (upstream and downstream of the BP), when irradiated with a mono-energetic 180 MeV/u ^{14}N ion beam is shown in figure 5. The stopper peak can be seen to occur at a lineal energy of ~ 900 keV/ μm . For the downstream depths, better agreement is observed between simulation and experiment compared to the case of the ^{12}C ion beam. This can be attributed to the smaller range of the ^{14}N beam, which is 100 mm less than the ^{12}C beam, leading to a reduced fragment build up curve and causing heavier fragments, such as boron, to have a much shorter range after the BP. The fragment energy peaks of the simulation and experiment again align well with one another and beyond 55 mm ^4He is the dominant fragment for both simulation and experiment.

A comparison between the experimental and simulated y_D and RBE_{10} are shown in figure 6. Good agreement is again seen between experiment and simulation, with downstream of the BP having much better agreement compared to ^{12}C due to the reduced contribution from larger fragments. The agreement between experiment and simulation is similar to the ^{12}C ion beam case, with agreement being $\sim 10\%$ for y_D before the distal BP and $\sim 2\%$ for RBE_{10} . The y_D has a value of ~ 28 keV/ μm at the entrance of the phantom and reaches a value of ~ 400 keV/ μm at the distal edge of the BP at ~ 50.5 mm depth. The RBE_{10} has a value of ~ 1.5 at the entrance of the phantom and reaches a maximum of ~ 3.1 just before the pinnacle of the BP. The RBE_{10} is seen to peak before the BP compared to the ^{12}C ion beam which peaks at the BP itself due to the higher LET of the ^{14}N ion beam causing over-killing effects to occur earlier along the Bragg curve.

3.3. Mono-energetic 400 MeV/u ^{16}O ion beam

The microdosimetric spectra in the case of a mono-energetic ^{16}O ion beam for various depths in the phantom are shown in figure 7. It should be re-iterated here that the ^{16}O ion beam had a 100 mm WET (corresponding to 86 mm of PMMA) placed approximately 300 mm before the phantom to shift the location of the BP in the water phantom. Despite the use of the range shifter the depths quoted here are with respect to the detector's position inside the water phantom. Comparing the microdosimetric spectra upstream of the BP, experiment and simulation agree well in terms of position and shape of the incident ^{16}O ion beam, with the stopper peak increasing to a higher lineal energy of ~ 1000 keV/ μm . Due to the larger range of the ^{16}O ion beam, the downstream microdosimetric spectra present a more similar trend to the ^{12}C ion beam than the ^{14}N ion beam, with a more noticeable over contribution of lighter fragments (with He fragments again being the most represented in the simulation).

The y_D and RBE_{10} values along the depth of the phantom are shown in figure 8. As with the previous beams, y_D gives an agreement of $\sim 10\%$ and $\text{RBE}_{10} \sim 2\%$, both before the distal edge of the BP, after the BP the discrepancy becomes larger due to the accuracy of the fragmentation model used (BIC). The y_D has a value of ~ 22 keV/ μm at the entrance of the phantom and increases to a value of ~ 320 keV/ μm just at the start of the distal edge of the BP at ~ 93 mm. The RBE_{10} has a value of 1.35 at the entrance of the water phantom and reaches a maximum of 2.9 just before the pinnacle of the BP due to over-killing. The values of y_D and RBE_{10} , at the surface of the phantom, for ^{16}O ions are slightly lower than ^{14}N ions. This is due to the much smaller range of ^{14}N causing less straggling to occur as well as a smaller contribution from fragments due to a reduced fragment build up curve.

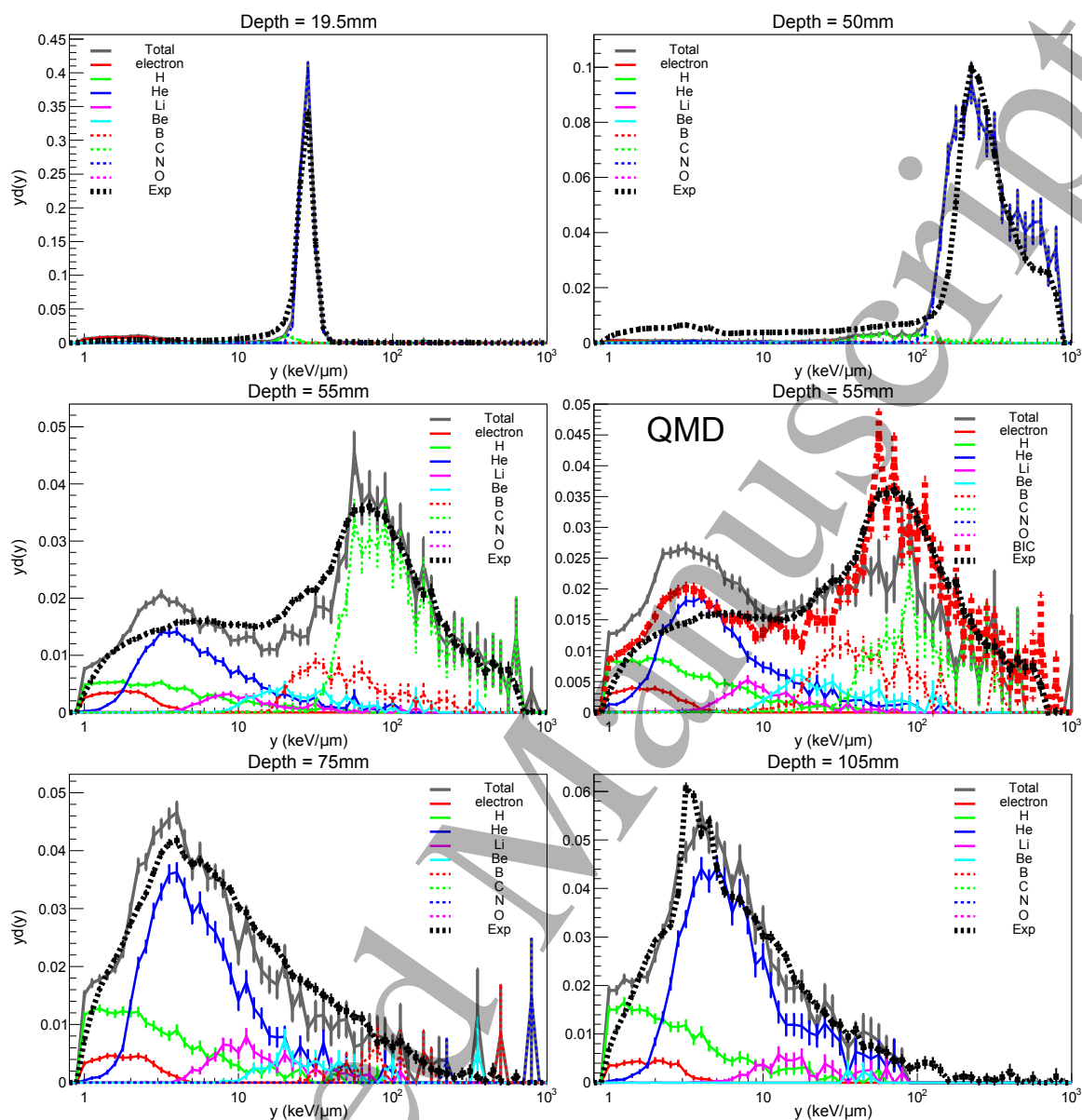


Figure 5: Comparison between the microdosimetric spectra calculated with Geant4 (continuous line) and the experimental measurements (dashed line) at different depths along a 180 MeV/u ^{14}N ion beam in a water phantom. All simulation spectra shown are obtained with the BIC model except for the 55 mm depth labelled with “QMD”, which was calculated with the QMD model.

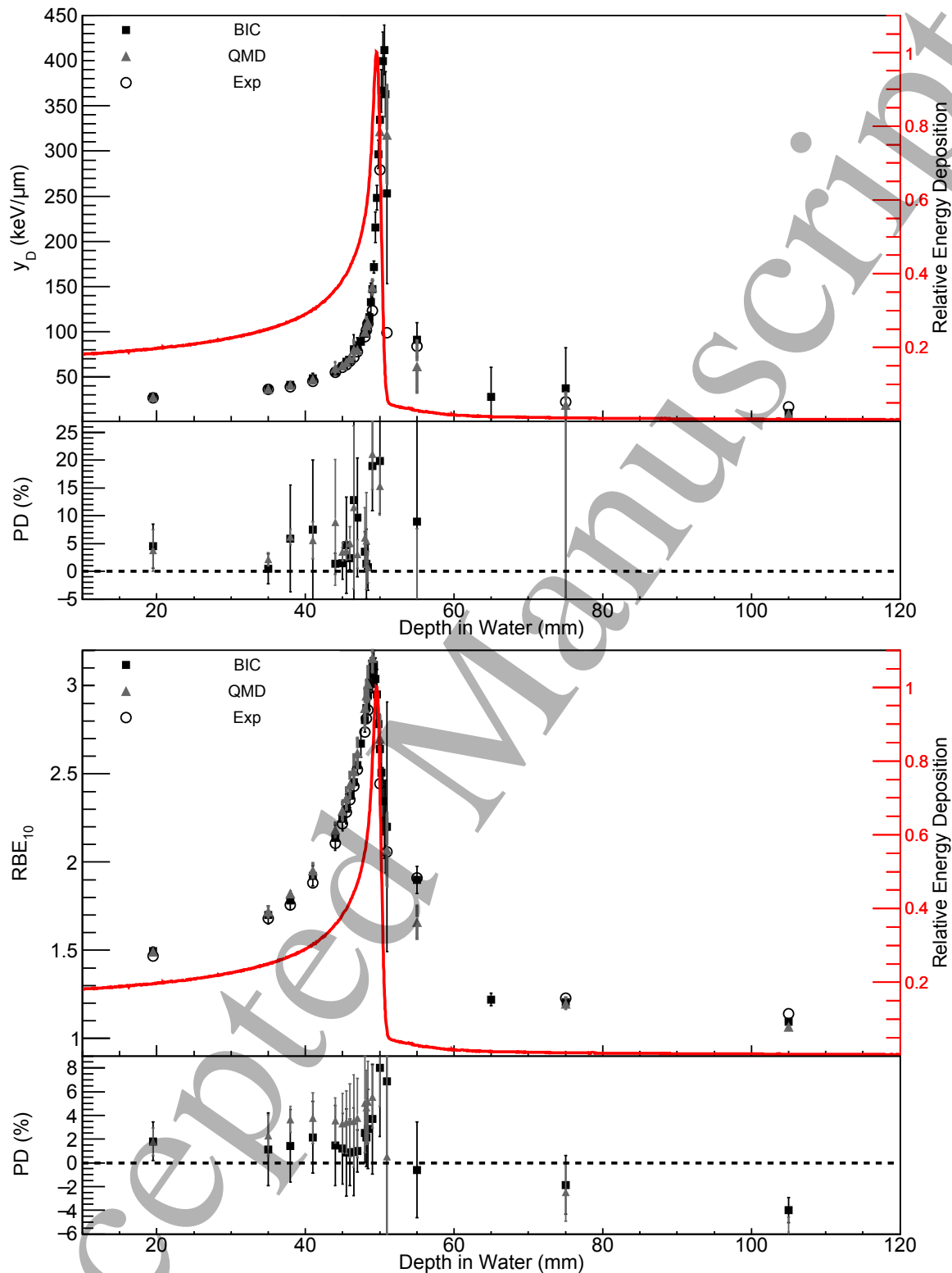


Figure 6: y_D (top) and RBE_{10} (bottom) values values in the 180 MeV/u ^{14}N beam using both the measured and simulated spectra from the Mushroom microdosimeter. The lower panels in both graphs show the percentage deviation (PD) between both data sets.

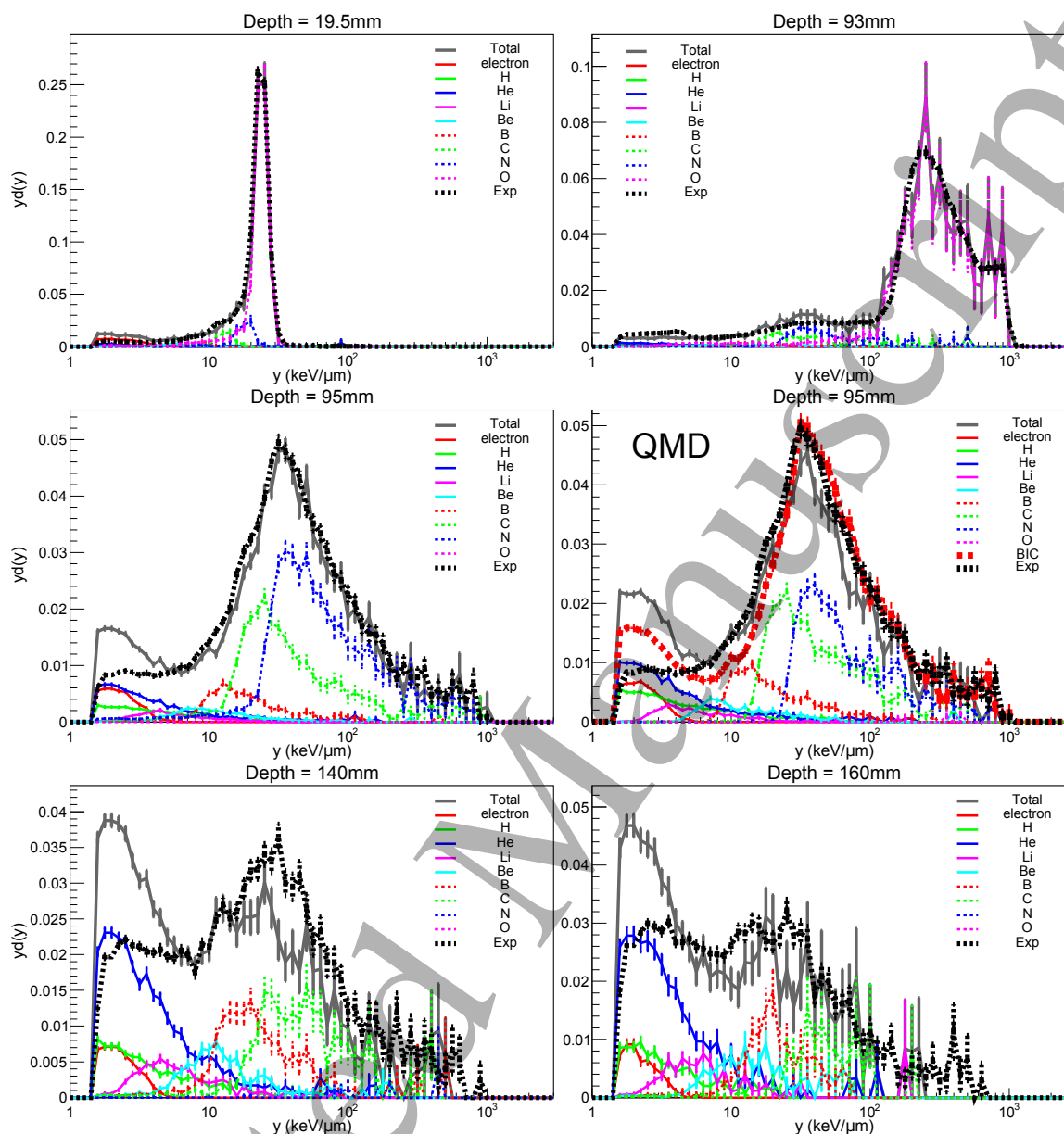


Figure 7: Comparison between the microdosimetric spectra of the simulated Mushroom detector and the experimental device when irradiated in a mono-energetic 400 MeV/u ^{16}O beam at various depths along the centre of the beam. All spectra are obtained with the BIC model except for the 95 mm depth on the right side which shows the response from QMD.

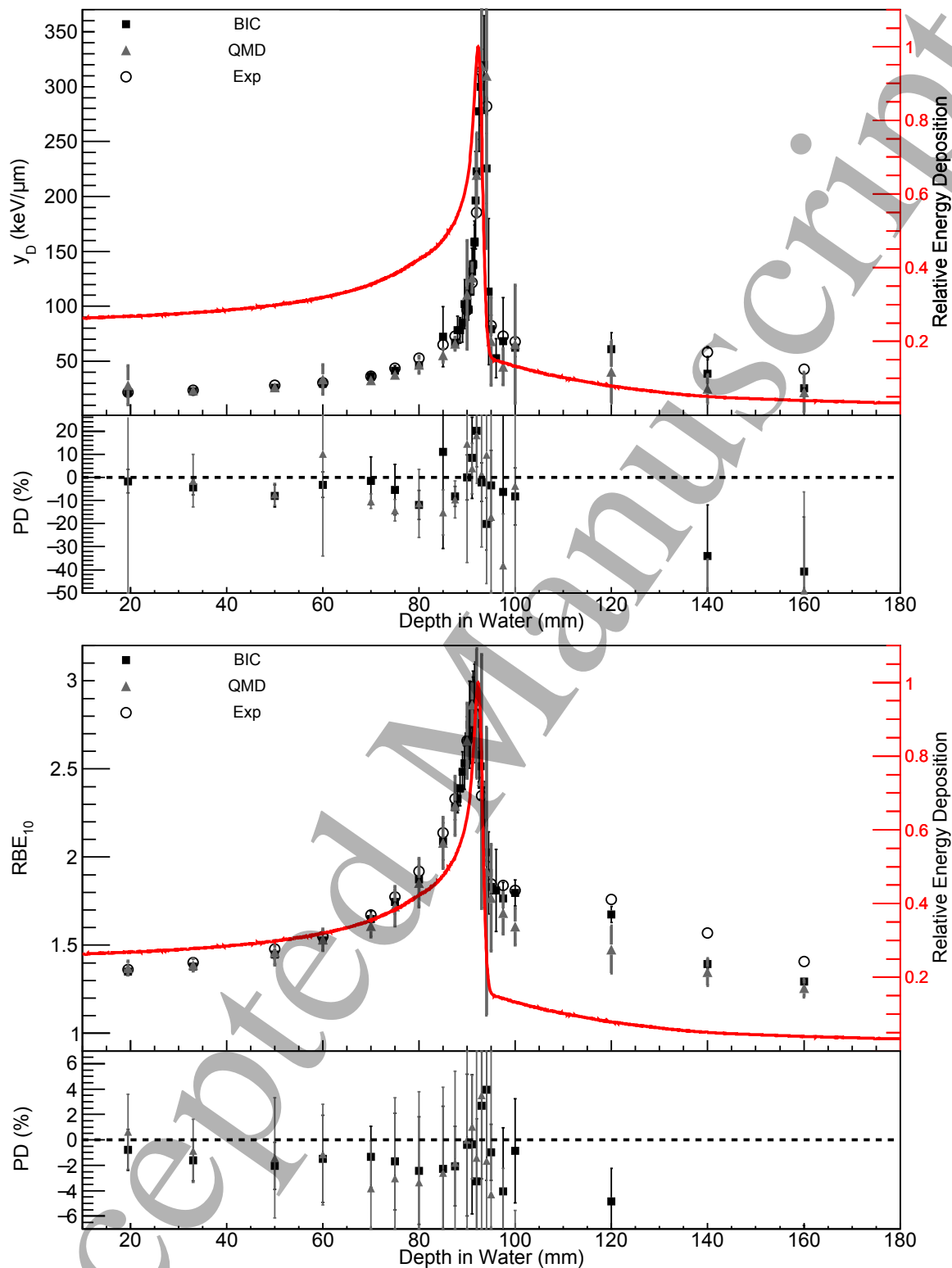


Figure 8: Calculated y_D (top) and RBE₁₀ (bottom) values in the 400 MeV/u ^{16}O beam using both the measured and simulated spectra from the Mushroom microdosimeter. The lower panels in both graphs show the percentage deviation (PD) between both data sets.

4. Discussion

As the incident primary ion traverses the target it will be attenuated based on its total reaction cross-section. As the primary ion beam attenuates it will produce different fragments based on the charge and mass changing cross-sections of the ion. The total reaction cross section of different projectiles and targets are well described in Geant4 and agree well with experimental measurements. The production cross sections of fragments are much more complex to describe due to not only needing to describe their production but also their angular and energy distributions. The ability of Geant4 to describe experimental measurements of the attenuation of a beam versus the production of fragments can be seen online (<https://geant-val.cern.ch/>), in particular the Charge Changing Cross-Section test (CCCStest), which compares the total and charge changing cross-sections in Geant4 for a ^{12}C ion beam. Additionally, the Hadron Data test (TestHD) compares the total reaction cross-section for various projectiles/targets and energies.

Due to the higher lineal energy of the incident primary beam compared to secondary fragments and its attenuation being fairly well described, the agreement between experiment and simulation is fairly consistent for all beams before the BP, with an agreement between $\sim 10\%$ for y_D and $\sim 2\%$ for RBE_{10} . As mentioned earlier, the RBE_{10} has noticeably less fluctuations than y_D due to their different dependence of the lineal energy spectra.

The observed agreement upstream reflects the dominance of the primary incident beam on the microdosimeter response, while the agreement downstream of the BP is dependent upon the model used and the fragments it generates. The alignment of the peaks of the microdosimetric spectra suggest that the model is adequate at generating the energy distribution of fragments. However, some discrepancies of the primary beam shape are seen between experiment and simulation, particularly on the left side of the peak. This is largely due to the charge collection of the device, where regions of the microdosimeter have a smaller charge collection efficiency compared to the majority of the SV region; charge collection maps of this device can be found in [20]. The effect of taking into account the charge collection distribution of the device in the simulation was investigated in [26] (chapter 6). It was found that the shape of the primary peak of the simulation was improved when applying the charge collection of the device but the spectra of the secondary fragments was less significantly impacted due to their large energy distribution compared to the primary ion beam.

Downstream of the BP for the ^{12}C and ^{16}O ion beams, which have a significantly larger range than ^{14}N which causes a greater fragment build-up as mentioned earlier, it was observed that there were more lighter fragments present in the simulation than experiment. This trend mimics the fragment study of [18], which compared the fragment distributions between experimental data [12] against Geant4 simulations for a 400 MeV/u ^{12}C ion beam incident upon a water target. The fragment study showed that, in general, larger fragments gave less agreement than lighter ones, in terms of the angular distribution. With larger fragments in the Geant4 simulation producing broader angular distributions compared to experimental measurements, this causes a greater proportion of larger fragments to leave the central beam axis compared to lighter fragments in the simulation. This effect is amplified further downstream of the BP, which is seen the most in this current work for the ^{16}O ion beam at 140 mm to 160 mm, where the disagreement increases.

Due to the dominance of the primary beam, the results do not differ significantly between BIC and QMD upstream of the BP, both in terms of the microdosimetric spectra and the y_D and RBE_{10} quantities. Downstream of the BP, QMD shows a greater contribution from lighter ions and BIC has a greater contribution of fragments with a charge of 1 less than the primary ion (Boron for ^{12}C , Carbon for ^{14}N and Nitrogen for ^{16}O). This trend was also observed in previous work [18], with QMD having a broader angular distribution of fragments compared to BIC. This results in QMD having slightly smaller values than BIC for y_D and RBE_{10} , as is most readily seen for ^{16}O which has the largest primary ion range. The lower values obtained

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7 with the QMD models result in larger differences between experiment compared to the BIC
8 model. An important consideration when choosing a model for Monte Carlo simulations is the
9 computational resources required. As reported previously in [18], the runtime of QMD for thick
10 targets was ~ 2 -8 times longer than the BIC model, for this study the observed increase in
11 runtime for most depths was mostly between 2-3 times longer. Due to this significant increase
12 in runtime for very little difference in results, particularly for positions where the primary ions
13 reach the detector, it can be difficult to justify the use of the QMD model over the BIC model
14 for the configuration studied here.

15 The agreement between experiment and simulation for values of y_D are similar to those found
16 in a study performed by Böhlen et al. [27], which compared the experimental microdosimetric
17 spectra of ^{12}C ion beams, measured using TEPCs, against simulation results of the FLUKA
18 code [28]. One of the experiments used to compare values of y_D against simulation was the
19 work of Martino et al. [29]. Agreement between the experimental measurements and FLUKA in
20 the work of Böhlen was within $\sim 4\%$ for y_D values for measurements at the centre of the beam
21 while those made 20 mm from the centre of the beam were within $\sim 11\%$. One notable difference
22 between the setup compared by Böhlen et al. and this study is that the beam size of ~ 2 -3
23 mm in diameter, and the size of the TEPC's SV chamber used was 12.7 mm in diameter. This
24 contrasts with the 100 mm diameter beam in this study and the 2500 SVs placed over an area
25 of $\sim 13 \text{ mm}^2$. The much larger beam size in this study may cause an increased contribution
26 in the detector response from fragments being directed outward from the primary path with
27 fragments generated laterally from the centre of the beam reaching the detector in the centre.
28 Additionally, the previous work used an active beam versus the passive beamline used in this
29 study. This means that the mixed radiation fields may have significant differences in terms of
30 fragment contribution.
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34 5. Conclusion

35 This work evaluated the performance of Geant4 to simulate the response of silicon
36 microdosimeters when irradiated with therapeutic ^{12}C , ^{14}N and ^{16}O ion beams. Simulation
37 results were benchmarked against published experimental measurements performed at the
38 HIMAC facility in Japan. Using a previously validated model of the HIMAC Biological beamline,
39 the silicon microdosimeter used in previous published experiments was accurately modelled and
40 irradiated using the beamline model.

41 The dose mean lineal energy (y_D) and the RBE_{10} , as estimated by the MKM, of each ion
42 beam was compared between simulation and experiment from upstream of the Bragg curve
43 to downstream of the fragment tail. Experimental measurements and simulation results agree
44 reasonably well along the primary ion beam. Due to the dominance of the primary ion beams
45 on the microdosimetric spectra, the agreement between experiment and simulation stayed fairly
46 constant before the BP with an agreement within $\sim 10\%$ for y_D and $\sim 2\%$ for RBE_{10} .

47 Downstream of the BP there was less agreement observed between simulation and experiment,
48 with the simulation having lower values of y_D and RBE_{10} due to the higher representation
49 of lighter fragments compared to heavier fragments. However, the ^{14}N beam gave fairly
50 good agreement downstream of the BP due to the smaller range of the beam causing lighter
51 fragments to dominate. Despite the contribution of fragments not giving the best agreement
52 between experiment and simulation, the lineal energy peaks of the fragment distributions
53 did give good agreement. The trends of fragments seen between simulation and experiment
54 from the Mushroom microdosimeter agree with the results from previous work, where angular
55 distributions of fragments were compared to experiment and showed larger fragments having
56 broader angular distributions.
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58 These results demonstrate that Geant4 is suitable for the simulation of silicon microdosimetry
59 in heavy ion therapy within $\sim 10\%$ for y_D and $\sim 2\%$ for RBE_{10} , as estimated by the MKM.
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Acknowledgement

This work was supported by computational resources provided by the Australian Government through the Raijin cluster under the National Computational Merit Allocation Scheme.

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