

Simple energy-budget model for yolk-feeding stages of Atlantic cod (*Gadus morhua*)

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Abstract

Atlantic cod (*Gadus morhua*) is a commercially important species, and therefore, understanding the influence of environmental factors and anthropogenic stressors on its early life stages is of considerable relevance. In this contribution, we apply a simple and generic energy-budget framework (DEBkiss) to data for the yolk-feeding stages of cod. The model is capable of explaining the changes in yolk volume, dry weight, oxygen use and body length, simultaneously with a small number of parameters. The calibrated model was subsequently successfully tested with other data sets. Interestingly, the light conditions after hatching affect growth and respiration rates, which is traced to a change in the maintenance costs (linked to swimming activity). Despite the satisfactory performance of the model, several uncertainties remain. Especially the bioenergetics around the point of complete yolk absorption require further attention, which is complicated by the fact that the behaviour around this point differed between data sets. The presented model can be used for exploring effects of stressors on early-life stages of cod, and

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likely for other aquatic egg-laying species as well.

Keywords: energy budget, DEBkiss, *Gadus morhua*, embryonic development, modelling, yolk absorption

1. Introduction

Atlantic cod (*Gadus morhua*) is a fish species of substantial economic importance, and therefore there is considerable interest in the effects of environmental factors and stressors (such as temperature and xenobiotics) on its life history. The early-life stages of fish are crucial for recruitment of both natural and cultured fish stocks (Kamler, 2008), and are regularly specifically sensitive to chemical stress (see e.g., Petersen and Kristensen, 1998; Massei et al., 2015). Interpreting, understanding and ultimately predicting stressor effects on the life history requires bioenergetic models (Jager et al., 2013). In all animals, food is used to fuel the energy-demanding processes of maintenance, activity, growth, development and reproduction. In doing so, the individual needs to obey the conservation laws for mass and energy, which helps to structure the modelling efforts.

The yolk-feeding stages are of particular interest from a bioenergetic viewpoint as most of them can be considered as semi-closed systems (Heming and Buddington, 1988): practically all of the energy that the developing embryo uses for its development is locked inside the egg in the form of endogenous yolk. This makes them ideal objects to study the effects of environmental factors and stresses on their energy budget. Specific bioenergetic models have been proposed for fish development over the yolk-feeding stages (Beer and Anderson, 1997; Jaworski and Kamler, 2002), but we aim for a more

22 general treatment, embedding the yolk stages into the rest of the life cycle
23 and linking fish to other animal species. Dynamic Energy Budget (DEB)
24 theory (Jusup et al., 2017; Sousa et al., 2010) offers such a generic and in-
25 clusive bioenergetics representation, covering the entire life cycle (from egg
26 to death) for all forms of life. The DEBkiss framework (Jager et al., 2013;
27 Jager, 2016) is derived from DEB theory by applying several simplifications
28 to ease parameterisation, interpretation and practical applications, such as
29 in interpreting the effects of chemical stress (Barsi et al., 2014) and ocean
30 acidification (Jager et al., 2016).

31 The most prominent simplification in DEBkiss is the removal of ‘reserve’
32 as a state variable in the model. For many applications, this turns out to
33 be an acceptable simplification (see list of papers at [http://www.debttox.](http://www.debttox.info/debkiss_appl.html)
34 [info/debkiss_appl.html](http://www.debttox.info/debkiss_appl.html)). The result is a simple model for bioenergetics
35 of (ectothermic) animals over their entire life cycle, including the embryonic
36 stages (Jager et al., 2013; Barsi et al., 2014). However, for eggs, the removal of
37 reserve required some additional thought. DEB theory considers the yolk as
38 part of the reserve, and clearly, no model for embryo bioenergetics can work
39 without a state variable that considers yolk. In DEBkiss, yolk is treated as
40 a buffer, handed over by the mother to the egg, which is assimilated, in a
41 similar fashion as assimilation of food by the free-swimming feeding stages.
42 This assumption is quite similar to the assumptions made for yolk absorption
43 by Beer and Anderson (1997) and Jaworski and Kamler (2002).

44 To test the performance of the simple DEBkiss model for egg development
45 and yolk feeding, we apply it to data for the Atlantic cod. Once parameterised
46 and tested, this model may prove to be useful to interpret and predict the

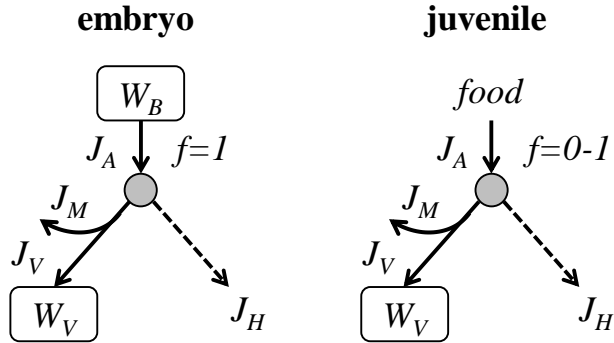


Figure 1: Schematic representation of the DEBkiss model for embryos and juveniles; in a DEB context, the transition from embryo to juvenile is defined by the start of (the ability for) external feeding. State variables are egg buffer or yolk (W_B) and structure (W_V), and fluxes are for assimilation (J_A), maintenance (J_M), growth (J_V) and maturation (J_H). The scaled functional response f is 1 for embryos (*ad libitum*) and depends on food availability for juveniles (zero when no food is present). Grey circle is a split of the assimilation flux, with a fraction of κ allocated to maintenance and growth.

47 effects of environmental changes and stressor effects on the yolk-feeding stages
 48 of cod. As the DEBkiss model is generic, it can then likely be applied to other
 49 fish species (and even other egg-laying animals) as well.

50 2. Methods

51 2.1. Basic model for embryos

52 A detailed description of DEBkiss can be found elsewhere (Jager et al.,
 53 2013; Jager, 2016); below a summary is given as far as relevant for the early
 54 life stages (reproduction is excluded from the model description here). The
 55 model structure for these stages is schematically shown in Figure 1, and all
 56 symbols used in this study are summarised in Table 1. Note that in DEB
 57 terminology, the embryo is the initial stage of the life cycle where the animal

58 does not feed exogenously, and the juvenile stage starts with the ability to
 59 feed exogenously. The points of hatching and metamorphosis (the end of
 60 the larval stage) are not stage switches from an energetic viewpoint.

61 Over its early development, the embryo goes through a series of events,
 62 for cod described in detail by [Hall et al. \(2004\)](#). These events represent
 63 major changes in morphology of the embryo, but for our DEBkiss model,
 64 all this detail will be ignored. The egg is treated as consisting of two state
 65 variables: the mass of the egg buffer W_B (representing the yolk) and the mass
 66 of structure W_V (representing the embryo or larvae without the yolk sac).
 67 The egg buffer is assimilated at a rate J_A , and structural mass increases with
 68 a growth flux J_V :

$$\frac{d}{dt}W_B = -J_A \quad \text{until } W_B = 0, \text{ with } W_B(0) = W_{B0} \quad (1)$$

$$\frac{d}{dt}W_V = J_V \quad \text{with } W_V(0) = W_{V0} \quad (2)$$

69 To facilitate the links between mass, surface area, and body length, it is
 70 practical to work with volumetric length (L), which is the cubic root of
 71 structural volume (using the dry-weight density d_V). Volumetric length can
 72 in turn be linked to more practical length measures (L_w , e.g., standard length,
 73 SL, in fish) by a shape-correction coefficient (δ_M):

$$L^3 = \frac{W_V}{d_V} \quad \text{and } L_w = \frac{L}{\delta_M} \quad (3)$$

74 Reported water content for cod larvae (4.5-10 mm SL) is around 85% ([Finn](#)
 75 [et al., 2002](#)). This implies that we can use $d_V = 0.15 \text{ mg/mm}^3$ as a reasonable
 76 estimate for the density of structure. In our calibration data set ([Finn et al.](#),

77 1995), yolk is expressed as a volume, and hence we also need a dry-weight
78 density for the egg buffer (d_B). We leave this as a free parameter to be
79 estimated in the fit to the data, as we have no direct information on the yolk
80 properties. Measurements on total fresh eggs (Finn et al., 1995) suggest a
81 value close to 0.07 mg/mm^3 .

82 Next, we need to fill in the mass fluxes for the various processes. The
83 assimilation flux (J_A) is proportional to a surface area of the animal, and
84 the maintenance flux (J_M) to a volume. A fraction κ of the assimilation flux
85 is used (with a certain efficiency, y_{VA}) for growth (J_V); the remainder (here
86 denoted as J_H) is assumed to be dissipated. In the DEB context, the flux J_H
87 is used for maturity and maturity maintenance; even though these processes
88 are not explicitly followed here, specification of this flux is needed to close
89 the mass balance and for the calculation of respiration rates later on. The
90 mass fluxes are defined as follows:

$$J_A = f J_{Am}^a L^2 \quad (\text{if } W_B > 0 \text{ then } f = 1) \quad (4)$$

$$J_M = J_M^v L^3 \quad (5)$$

$$J_V = y_{VA}(\kappa J_A - J_M) \quad (6)$$

$$J_H = (1 - \kappa) J_A \quad (7)$$

91 The scaled functional response f is included in the assimilation flux J_A , and
92 is a function of food availability (1 represents *ad libitum* conditions and 0
93 complete starvation). For yolk-feeding stages, we assume $f = 1$ until yolk
94 runs out. However, what happens when the larva starts to feed exogeneously?
95 The larvae obtain the ability to feed after development of a functional jaw

96 and hindgut (Hall et al., 2004), which is generally before the yolk is fully
97 exhausted (Kamler, 2008; Heming and Buddington, 1988). This implies that
98 we, at some point, need to consider two food sources. We leave the question
99 of mixed feeding open at the moment, as the experimental data sets that we
100 use did not offer any food to the animals. The resulting instantaneous switch
101 from $f = 1$ to $f = 0$ is unrealistic in detail; in practice, we will likely see a
102 smoother transition from yolk-feeding to starvation.

103 *2.2. Response to starvation and temperature*

104 When the allocated assimilation flux κJ_A is insufficient to cover the main-
105 tenance costs J_M , the animal needs to deviate from the rules provided above.
106 Jager et al. (2013) proposed a simple model to deal with this problem in two
107 stages (see supporting information). Here, we can simplify the model to a
108 single stage as we assumed an instantaneous switch from $f = 1$ to $f = 0$
109 when yolk runs out. In the absence of yolk or external food, the animal will
110 shrink, i.e., use structural tissue to pay the maintenance cost:

$$J_V = -J_M/y_{AV} \text{ and } J_H = 0 \quad (8)$$

111 Shrinking (negative value for J_V) implies that W_V will decrease, but not nec-
112 essarily L_w . If we use standard length as our size measure, it will be deter-
113 mined by the length of the notochord, which is unlikely capable of shrinking.

114 Temperature is clearly an important factor for the bioenergetics, and
115 increasing the temperature speeds up development (Geffen et al., 2006). In
116 DEB applications, it is generally assumed that all rate constants (with a
117 dimension that includes ‘per time’) scale in the same way with temperature.

118 We can use the Arrhenius relationship to scale from a reference temperature
 119 T^* to the actual temperature T (both in Kelvin). All rate constants have to
 120 be multiplied by:

$$F_T = \exp\left(\frac{T_A}{T^*} - \frac{T_A}{T}\right) \quad (9)$$

121 where T_A is the Arrhenius temperature in Kelvin. [Lika et al. \(2011\)](#) suggest
 122 a value of 8000 K as typical value.

123 *2.3. Link between mass fluxes and oxygen use*

124 Measurements of oxygen use provide valuable insights into the bioener-
 125 getics of the yolk-feeding stages. They are easier to interpret than mea-
 126 surements on the externally-feeding stages: the embryos continue all of the
 127 regular metabolic work during the measurement of oxygen use, as they have
 128 a constant supply of energy. In contrast, feeding stages will usually be fasted
 129 for some time before measurement, with unclear consequences for the bioen-
 130 ergetics (see [Jager and Ravagnan, 2016](#)). Oxygen use is related to the mass
 131 fluxes that dissipate. The total dissipation flux (J_D), as relevant in the con-
 132 text of the early life stages, is given by:

$$J_D = J_M + J_H + J_{V_o} \quad (10)$$

133 Where J_{V_o} indicates the overhead costs for growth or shrinking:

$$J_{V_o} = \begin{cases} J_V(1 - y_{VA})/y_{VA} & \text{if } J_V \geq 0 \\ J_V(y_{AV} - 1) & \text{if } J_V < 0 \end{cases} \quad (11)$$

134 The dissipation flux is a mass flux (in mg of assimilates per day). In practice,
 135 respiration is often expressed in terms of oxygen use. To convert this mass

136 flux to moles of oxygen, we need the carbon content of biomass or yolk for the
137 species (d_C ; we take 0.4 mg/mg as a representative value), the molar mass of
138 carbon (12 g/mol), and the respiratory quotient (F_{RQ}). This quotient is the
139 moles of CO_2 (and thus also the moles of C) eliminated per mole of O_2 taken
140 up (we take 0.8 as a reasonable value). For our validation study, we need
141 to convert moles of oxygen further to microliters, which requires the molar
142 mass of oxygen (32 g/mol) and its density (1.43 g/L at 0°C).

143 *2.4. Implementation and calibration*

144 The model was implemented in Matlab using the generic BYOM plat-
145 form (<http://www.debttox.info/byom.html>). Optimisation was performed
146 by maximising an overall likelihood function (assuming normally-distributed
147 and independent errors). Confidence intervals were calculated by profiling the
148 likelihood. All data were extracted from the original publications using the
149 freeware PlotReader (<http://jornbr.home.xs4all.nl/plotreader>). The
150 data are used in the form, and with the units, as given in the original pub-
151 lications; the model outputs (W_B , W_V and J_D) were recalculated to match
152 the type and unit of the data set. This is done to keep the data points un-
153 affected by the uncertainty in the transformations. The only recalculation
154 is the derivation of yolk dry weight in the data sets of [Solberg and Tilseth](#)
155 ([1984,?](#)). This is calculated from the total weights for eggs/larvae and chorion
156 weight (and thus requires no uncertain transformations).

157 We selected the data set from [Finn et al. \(1995\)](#) to calibrate the model,
158 as it contains measurements on different endpoints from the same group of
159 animals: yolk volume, dry weights, standard length (after hatch), and respi-
160 ration rate. The experiments were performed at 6°C , with the eggs initially

161 kept under continuous light, but switching to a 14:10 light-dark regime post
162 hatching. The measured dry weight of the complete egg requires some fur-
163 ther thought as this measurement includes contributions from the yolk, the
164 structural part of the embryo, and the chorion of the egg. For the chorion,
165 we take a fixed value of 0.020 mg, based on the measurements of [Solberg and](#)
166 [Tilseth \(1984\)](#).

167 For the respiration data, two series of measurements were presented: one
168 in light and one in dark conditions. For the egg stage and several days af-
169 ter hatching, these measurements were very similar, but around the time
170 that yolk ran out, a profound difference was observed. A square-root trans-
171 formation was applied for this data set to increase the importance of the
172 initial respiration measurements of the early egg stages, and decrease the
173 importance of the post-hatching measurements (which is useful in view of
174 the variation induced by light conditions).

175 *2.5. Model testing*

176 To test the model and its parameterisation, a second (independent) data
177 set ([Solberg and Tilseth, 1984](#)) was used as model corroboration. These
178 authors report measurements of dry weights of chorion, total egg, whole
179 larvae (incl. yolk), larvae with dissected yolk, as well as standard length
180 post hatch. These experiments were performed at 5°C under a 12:12 hour
181 light regime, and used two batches of eggs from different females. Since these
182 experiments were done at a slightly different temperature (5°C instead of
183 6°C), we calculated a temperature correction factor (Eq. 9), which is applied
184 to both rate constants (specific assimilation and specific maintenance rates).

185 The initial amount of yolk (W_{B0}) was calculated from the mean weight of

186 the total fresh egg in this study (0.107 mg) minus the chorion and the value
187 of W_{V0} (Table 1). Additionally, the same study reports some respiration
188 data, post-hatching, from other batches of eggs. We added the respiration
189 data from [Serigstad and Adoff \(1985\)](#), which covers the egg stage as well
190 (also performed at 5°C). For all respiration data sets, we do not have the
191 corresponding development of larval and yolk mass for the same batches of
192 eggs, which implies additional uncertainty.

193 *2.6. Effects of light and temperature*

194 [Solberg and Tilseth \(1984, 1987\)](#) also report an experiment with hatched
195 larvae, reared under different temperatures (3, 5 and 7°C) and light condi-
196 tions (constant darkness or constant light). Total dry weight, dry weight
197 of larvae with dissected yolk, and standard length were reported. Initial
198 amounts of yolk and structure were fixed to the first measurements (shortly
199 after hatching). These data only have information for the end of the yolk-
200 feeding stage and the subsequent starvation phase. We fitted both the specific
201 assimilation rate and the specific maintenance rate on each treatment (κ was
202 fixed to the value established in the calibration, see Table 1), and only show
203 the parameter estimates (fits are provided in supporting information).

204 **3. Results and discussion**

205 *3.1. Model calibration*

206 The model fit to the calibration data ([Finn et al., 1995](#)) is shown in Figure
207 2. The four data sets are fitted simultaneously with only seven parameters;
208 an average of less than two parameters per data set (parameter estimates

Sym.	Explanation	Value (C.I.)	Unit
Primary parameters			
f	Scaled functional response	1/0 (n.e.)	–
J_{Am}^a	Maximum area-specific assimilation rate	16.0 (14.7-17.1) 10^{-3}	mg mm ⁻² d ⁻¹
J_M^v	Volume-specific maintenance costs	4.37 (3.87-5.02) 10^{-3}	mg mm ⁻³ d ⁻¹
y_{AV}	Yield assimilates on structure (shrinking)	0.8 (n.e.)	mg mg ⁻¹
y_{VA}	Yield structure on assimilates (growth)	0.8 (n.e.)	mg mg ⁻¹
κ	Fraction of assimilation flux for soma	1 (0.949-1)	–
Initial states			
W_{B0}	Assimilates in freshly-laid egg	100 (96.9-104) 10^{-3}	mg
W_{V0}	Structure in freshly-laid egg	2.35 (1.48-3.64) 10^{-3}	mg
Conversions			
d_B	Dry-weight density of egg buffer	0.0745 (0.0714-0.0796)	mg mm ⁻³
d_C	Carbon content of yolk and structure	0.40 (n.e.)	mg mg ⁻¹
d_V	Dry-weight density of structure	0.15 (n.e.)	mg mm ⁻³
F_{RQ}	Respiratory quotient	0.8 (n.e.)	–
W_c	Weight of chorion of egg	0.020 (n.e.)	mg
δ_M	Shape correction coefficient	0.157 (0.151-0.162)	–
Fluxes and state variables			
J_A	Mass flux for assimilation		mg d ⁻¹
J_D	Total mass flux that is dissipated		mg d ⁻¹
J_H	Mass flux for maturation/maturity maint.		mg d ⁻¹
J_M	Mass flux for maintenance		mg d ⁻¹
J_V	Mass flux for structure (growth/shrinking)		mg d ⁻¹
J_{Vo}	Overhead costs for growth/shrinking		mg d ⁻¹
W_B	Mass of assimilates buffer in egg		mg
W_V	Mass of structural body		mg
Derived or intermediate variables			
L	Volumetric body length		mm
L_w	Physical body length (e.g., SL)		mm

Table 1: Explanation of symbols used in this study. For parameters and constants, values are given, which are either fitted (see Fig. 12; , 95% confidence interval in parentheses) or fixed (n.e., not estimated). Values for the yield coefficients are taken from Jager et al. (2013); other fixed values explained in the text. When yolk is present $f = 1$, and otherwise $f = 0$. Rate constants represent a temperature of 6°C.

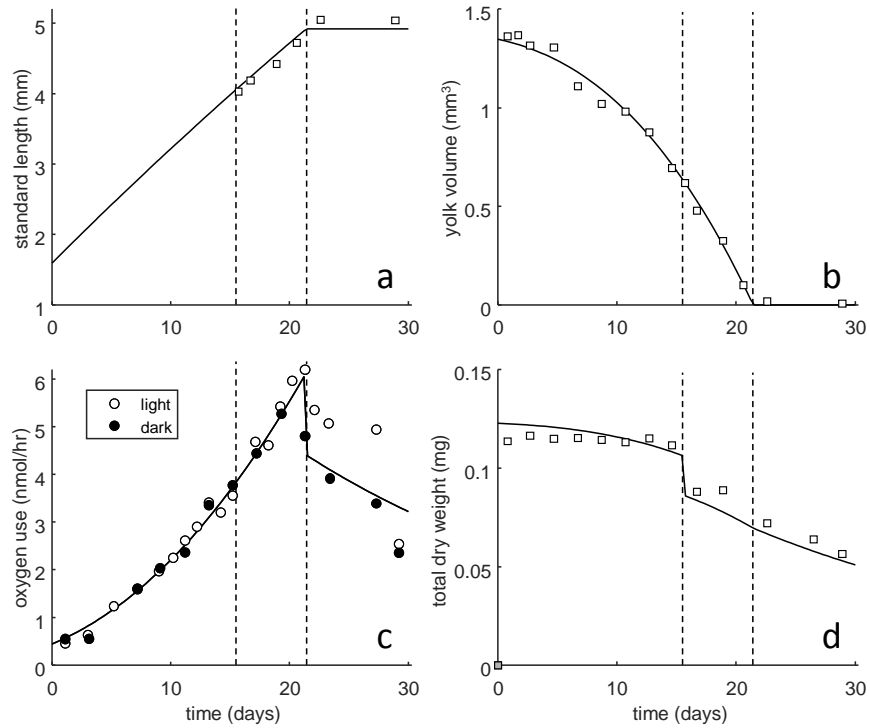


Figure 2: Fit of the DEBkiss model on data from Finn et al. (1995) at 6°C. For the respiration plot (panel c), different symbols are used for measurements under light or dark conditions. The first broken line indicates the approximate time for hatching in the experiment, and the second broken line represents the modelled time for total yolk absorption. The jump in dry weight is the loss of the chorion at hatching (chorion weight taken as 0.020 mg).

209 with confidence intervals are given in Table 1). The model itself has only
210 three parameters that need to be fitted. Additionally, there are two initial
211 states (initial mass of structure and yolk) that need to be estimated, as well
212 as two conversion factors to link state variables (mass) to observations (yolk
213 volume and standard length). Note that the estimate for the density of yolk
214 is very close to the value estimated from the total fresh egg (0.07 mg/mm³;
215 Finn et al., 1995).

216 Overall, the fit is very good, but several issues can be observed on closer
217 inspection. Starting with the total dry weight (Fig. 2d): the model predicts
218 a decrease of total dry weight over the egg stage, which is not shown in
219 the data. As the egg membrane severely restricts uptake of solutes, the
220 burning of yolk (mass flux J_D) should lead to a loss of dry weight as the
221 embryo develops (closely linked to the observed respiration rate). Eggs may
222 be taking up some minerals from water, but no increase in ash content was
223 observed in this study (Finn et al., 1995). Further, eggs and larvae appear
224 to be capable of absorbing dissolved organic molecules from water, although
225 the contribution to the mass and energy budget is expected to be negligible
226 (Heming and Buddington, 1988). A decrease in total egg weight was observed
227 in the validation data set (Solberg and Tilseth, 1984), so the lack of a decrease
228 here could represent a measurement bias.

229 The respiration rate (Fig. 2c) is nicely fitted up to the point where the
230 yolk runs out. At that point, there is also a clear difference between the res-
231 piration rate measured in light and in dark conditions. The model predicts
232 a sharp drop in respiration rate when yolk runs out, as the scaled functional
233 response switches instantly from $f = 1$ to $f = 0$. As a result of this transition

234 to complete starvation, growth switches to shrinking to match the mainte-
235 nance needs, which leads to a lower total dissipation flux. As starvation
236 progresses, respiration decreases as also the total amount of structure to be
237 maintained decreases. This pattern is, in general, consistent with the data,
238 although there is a considerable difference between the respiration data in
239 light and dark conditions. The animals in the light clearly have a higher
240 respiration rate after complete yolk absorption than predicted, which can be
241 linked to an increased swimming activity (see [Solberg and Tilseth, 1984](#)).
242 The role of swimming activity in the energy budget is discussed further in
243 Section [3.3](#).

244 The increase in standard length over time (Fig. [2a](#)) is well matched by
245 the model (note that animals cannot shrink in length, even though they
246 do shrink in dry weight). However, growth seems to increase for slightly
247 longer than predicted. This might be caused by experimental difficulties of
248 accurately measuring yolk volume close to the point of complete resorption.
249 It is also possible that some resources have already been irreversibly allocated
250 to length increase (notochord growth).

251 The estimate for κ is very high; virtually all of the assimilated energy
252 from yolk is used for maintenance and growth. This value is linked to the
253 fixed value for the growth efficiency (y_{VA}), and to the estimated specific
254 maintenance rate (J_M^v), which in turn relies on the assumption that the
255 shrinking of the larvae is linked to the maintenance requirements only. Given
256 that the specific assimilation rate is severely restricted by the observed yolk
257 absorption, these three parameters (κ , y_{VA} and J_M^v) determine the three
258 fluxes contributing to dissipation (see Eq. [10](#)), and hence the efficiency with

259 which yolk is turned into structural biomass. For example, assuming a higher
260 growth efficiency ($y_{VA} = 0.90$) allows κ to decrease ($\kappa = 0.93$), with very
261 little effect on the goodness-of-fit. It will be difficult in practice to determine
262 the value of the yield coefficients, although this is unlikely to affect practical
263 applications of the model.

264 The estimated value for the specific maintenance rate is very similar to
265 the values established for two krill species (Jager and Ravagnan, 2016), when
266 using the same reference temperature (assuming an Arrhenius temperature of
267 8000 K). The specific assimilation rate is, however, lower, which is surprising
268 as cod will obviously grow to much larger sizes than krill (maximum volu-
269 metric length is determined by $\kappa J_{Am}^a / J_M^v$). The solution to this conundrum
270 lies in the fact that fish accelerate metabolically after the start of feeding
271 (Kooijman et al., 2011), which involves an increase of the specific assimila-
272 tion rate for some time after yolk has disappeared. This allows these species
273 to reach much larger sizes than indicated by their embryonic stage, and also
274 explains the deviation from von Bertalanffy growth when early stages are
275 included in the growth curve. Such an acceleration of growth (relative to
276 von Bertalanffy growth) was observed for larval cod by Otterlei et al. (1999)
277 as a clear up-curving for the length-age relationship.

278 3.2. Model testing

279 Next, the parameterised model is tested with data from Solberg and
280 Tilseth (1984). The correspondence between model and data is quite con-
281 vincing (Fig. 3), especially given the fact that no parameters are fitted.
282 Interestingly, development in this study (and for the additional respiration
283 data from Serigstad and Adoff, 1985, in panel c) was somewhat slower than

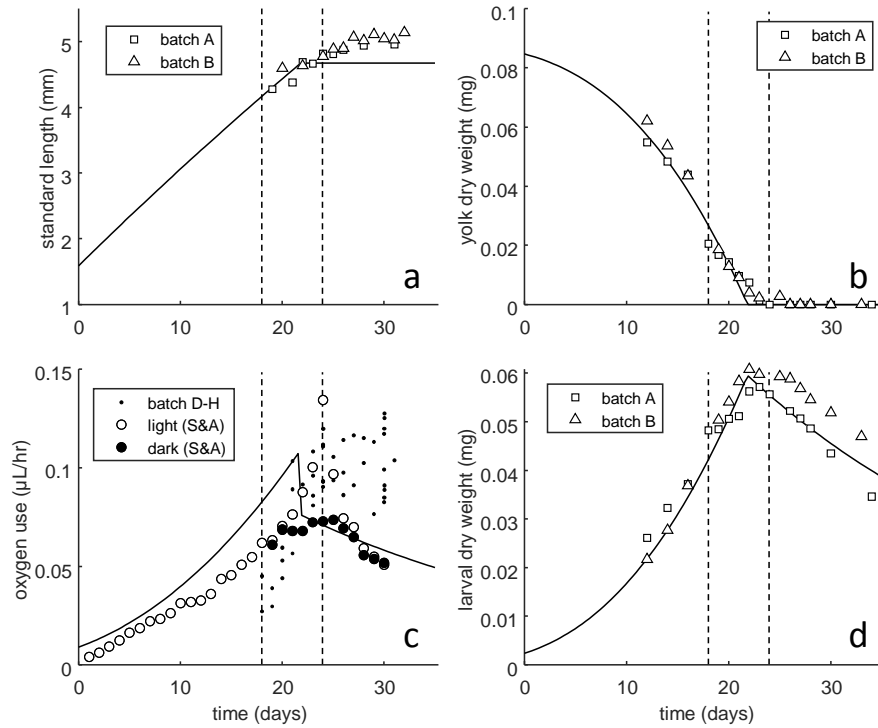


Figure 3: Predictions for additional data (Solberg and Tilseth, 1984) with different batches of eggs at 5°C. The respiration data light/dark (panel c) are taken from Serigstad and Adoff (1985). The model parameters were fixed to the best-fitting values from Table 1, with a temperature correction using Eq. 9. The broken lines indicate the approximate times for hatching and total yolk absorption, as observed in these experiments.

284 in the calibration study (Fig. 2). Hatching took place around day 18 (com-
285 pared to day 16 in the calibration study), and complete yolk absorption after
286 24 days, or even later (compared to 21 days in the calibration). Further-
287 more, the final stage of yolk resorption seems to be somewhat slower than
288 predicted from the model (Fig. 3b). It appears that the transition from
289 *ad libitum* yolk feeding to complete starvation is more gentle than assumed
290 in the model. Also, growth in length (Fig. 3a) continues for quite a while
291 longer than predicted. These deviations from the model predictions were
292 not observed to the same extent in the calibration data set (Fig. 2). It
293 is tempting to include smoothing mechanisms, such as the internal reserve
294 compartment of the standard DEB model (Sousa et al., 2010) or a limitation
295 of the assimilation flux by the surface area of the yolk sac (see Beer and An-
296 derson, 1997, and supporting information). However, such mechanisms are
297 inconsistent with the rather rapid transition in respiration rate when yolk
298 disappears (Fig. 2c), and were also not as clear in other batches of eggs from
299 Solberg and Tilseth (1984) (see supporting information). More detailed data
300 on growth and respiration would be needed to settle this question.

301 The respiration data from different batches of eggs (batch D-H in Fig. 3c)
302 are not well matched by the model prediction. Before final yolk absorption
303 the data are overestimated and afterwards underestimated. The reasons for
304 this discrepancy are unclear. The data set from Serigstad and Adoff (1985)
305 (with larvae reared under continuous light or darkness) shows a pattern that
306 better matches the model predictions, although the data are shifted to the
307 right, as already mentioned. Interestingly, the respiration data for constant
308 light show a closer resemblance to the pattern predicted by the model; hence,

309 the model suggests that respiration rates are depressed in darkness, rather
310 than being stimulated by light. Respiration rates are, however, difficult to
311 interpret without measurements for yolk and structural mass on the same
312 animals.

313 We can now also use the model to predict embryonic development under
314 other conditions. For example, we can predict how the duration of yolk feed-
315 ing will change with egg size. Model simulation shows that yolk feeding will
316 be extended by a factor of 1.4 longer for a doubling of the yolk content, which
317 is well in line with the factor of 1.3 mentioned by [Heming and Buddington](#)
318 (1988) for cod and herring.

319 *3.3. Effect of temperature and light*

320 The last data sets we used are also from [Solberg and Tilseth \(1984, 1987\)](#),
321 but consider only the changes in yolk weight, larval weight, and SL, post
322 hatching (in absence of food). These experiments were performed at three
323 temperatures and at constant light or constant darkness. All six data sets
324 were fitted, and the fitted parameters are plotted in Figure 4 (individual fits
325 shown in supporting information). The values for the specific maintenance
326 rate are well in line with the value determined earlier for 6°C (Table 1);
327 the calibrated value is in between the estimates for total light and total
328 darkness. However, the specific assimilation rates are roughly half of what
329 was estimated from the calibration data. This is likely linked to a slower use
330 of the final portion of the yolk, as discussed above (these six data sets only
331 follow the larvae when the yolk is already almost exhausted).

332 Specific assimilation rates are somewhat lower in the light, but the con-
333 fidence intervals mostly overlap. However, for the specific maintenance rate,

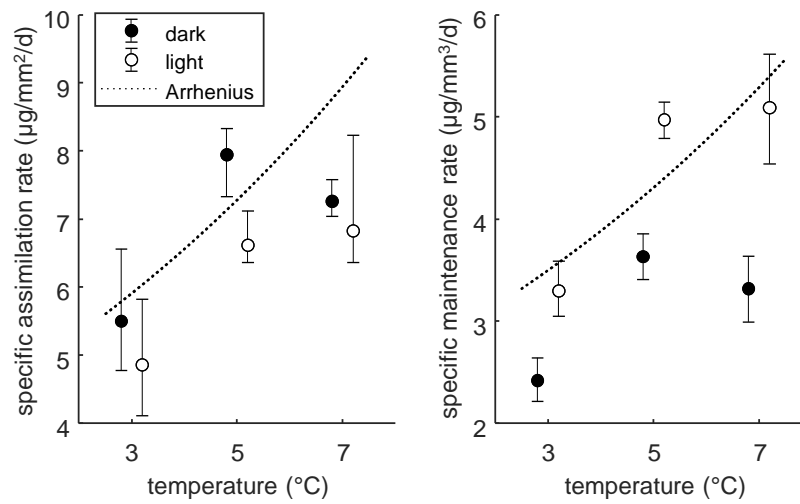


Figure 4: Parameter values with 95% confidence interval from fits on data for post-hatching development without food, at three temperatures and continuous light or darkness (Solberg and Tilseth, 1984, 1987). Points are slightly shifted horizontally to enhance readability. An Arrhenius relationship with an Arrhenius temperature of 8000 K is shown for reference. The κ was fixed to the value in Table 1.

334 there is a clearly elevated rate constant (on average 42% across the tested
335 temperatures) in the light at all temperatures. As shown in Figure 2c and
336 3c, animals kept in the light also showed higher respiration rates, which is
337 likely linked to their higher swimming activity (Solberg and Tilseth, 1984).
338 Thus, we can infer that swimming activity shows up in the energy budget as
339 a component of the maintenance rate. Since maintenance costs compete with
340 growth, and cause shrinking when the yolk has run out, they show up in the
341 pattern of structural body mass over time. In DEB models, the maintenance
342 rate is generally taken as a constant, lumping the energy requirements for
343 tissue maintenance and activity (Sousa et al., 2010). This assumption may
344 need some more detailed consideration, especially for fish larvae experiencing
345 a diurnal cycle.

346 Figure 4 also shows an Arrhenius relationship, going through the mean
347 value of each rate constant at 5°C. The increase in the rate constants from
348 3-5°C is consistent with this prediction, but there is no further increase to
349 be observed from 5-7°C. The reason for this lack of temperature effect is
350 unclear, but may relate to experimental problems. Interestingly, the data on
351 hatching time, provided in the same paper, do show a smoothly decreasing
352 relationship with temperature, as do the data sets provided in Geffen et al.
353 (2006) over a much wider temperature range.

354 4. Conclusions

355 We applied the generic energy-budget model DEBkiss to extensive data
356 for early life stages of cod. In general, this simple model provided an excel-
357 lent explanation of the data sets. Some aspects in some of the data indicate

358 the presence of a smoothing mechanism (delayed response of length growth
359 to yolk depletion, and decreased absorption rates when the yolk sac is very
360 small), but the rather rapid response of the respiration rate on yolk exhaus-
361 tion argues against it. Clearly, all models are wrong in detail, and simple
362 models, like energy-budget approaches, obviously lack many of the morpho-
363 logical (e.g., [Hall et al., 2004](#)) and biochemical (e.g., [Finn et al., 1995](#)) details.
364 In the end, the utility of these models must be judged in light of the specific
365 application for which they are used. The applications that we envisage for
366 this model are in the interpretation and prediction of the effects of (combi-
367 nations of) environmental factors and stressors on embryonic development.

368 The type of application that we specifically see is in the interpretation of
369 toxicity tests with embryos. This is particularly pertinent as toxicity tests
370 with embryonic fish are increasingly being used as alternatives for testing
371 with subsequent (and legally-protected) life stages (e.g., [Embry et al., 2010](#)).
372 Even though more-detailed evaluation will be needed, work on the effects of
373 acetone on pond-snail eggs ([Barsi et al., 2014](#)) already provided substantial
374 support. To apply the model to toxicants, it needs to be extended with a tox-
375 icokinetics module (see [Jager, 2016](#)). For eggs and yolk-feeding larval stages,
376 additional consideration will be necessary. For example, the rate of chemical
377 exchange for the egg stage is considerably slower than for the larvae post
378 hatching ([Petersen and Kristensen, 1998](#)). Furthermore, there may also be
379 stage-specific mechanisms of toxicity in the early life stages (see e.g., [Massei
380 et al., 2015](#)). It should furthermore be noted that energy-budget models are
381 of little help in the interpretation of non-energy related endpoints such as
382 malformations. Nevertheless, such endpoints will still require knowledge on

383 toxicokinetics, and it is likely that toxicokinetics is affected by the patterns
384 of structural and yolk mass over time.

385 In this study, we only considered the yolk-feeding stages. However, it is
386 good to realise that DEBkiss is a model for the full life cycle of animals.
387 Full-life cycle bioenergetic models have a range of potential applications, for
388 example in conjunction with individual-based population models (IBMs) to
389 assess population development under time-varying environmental conditions.
390 Models based on DEBkiss have been linked to IBMs in some cases, such as for
391 salmon (Fiechter et al., 2015) and krill Groeneveld et al. (2015). Even though
392 more work is needed to test the embryo-specific part of the model in detail,
393 the advantage of DEB-based approaches is that the embryonic stage is treated
394 in a manner that is consistent with the rest of the life cycle, and consistent
395 with other forms of life. The only cod-specific aspect of the model are the
396 parameter values. This generic approach to bioenergetics will generally be
397 a more efficient strategy in understanding and interpreting stressor effects
398 than developing a new model for each life stage and each species.

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